

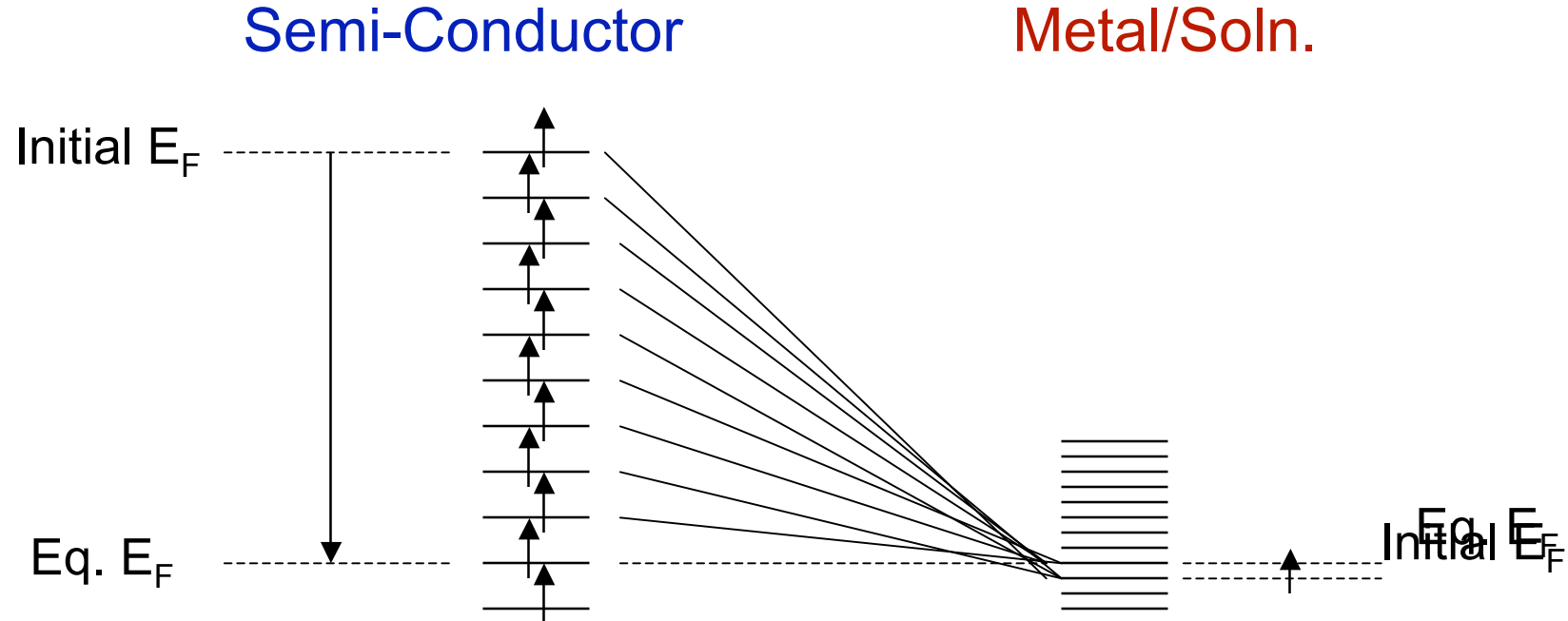
Chemistry 140a

Lecture #5

Jan, 29 2002

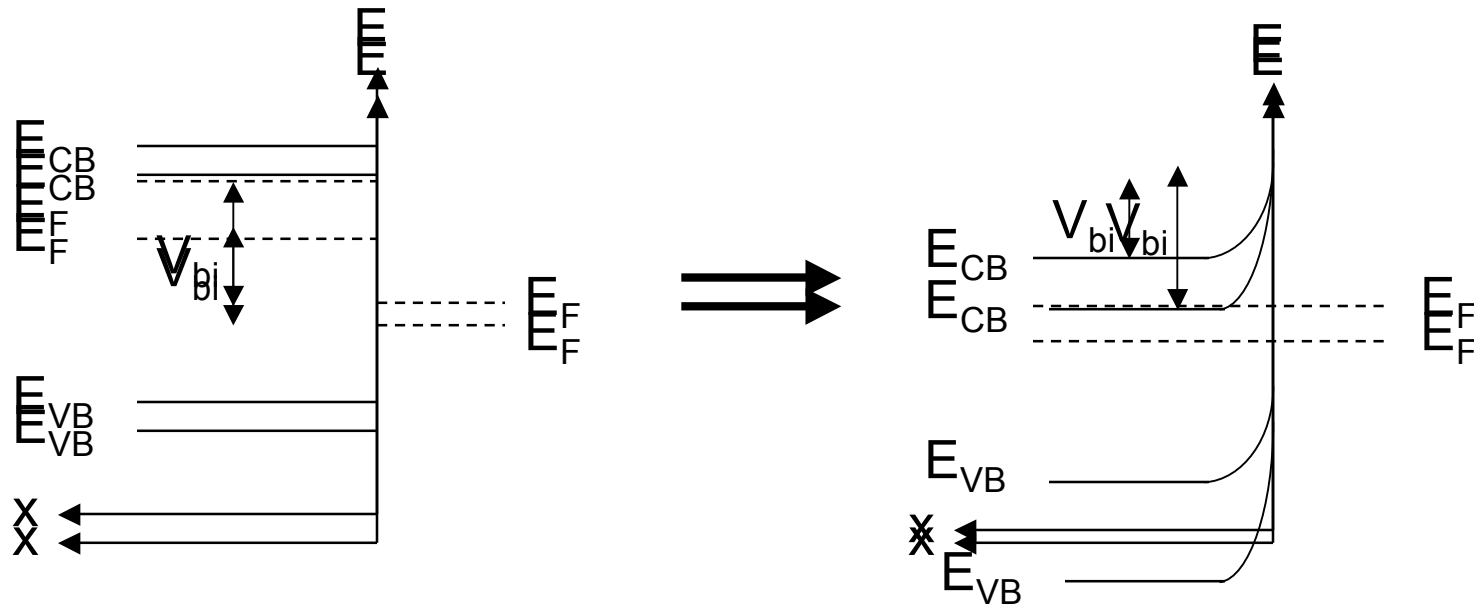
Fermi-Level Equilibration

- When placing two surfaces in contact, they will equilibrate; just like the water level in a canal lock.
- The E_F of the semi-conductor will always lower to the E_F of the metal or the solution. This can be understood by looking at the density of states for each material/soln.



Fermi-Level Equilibration

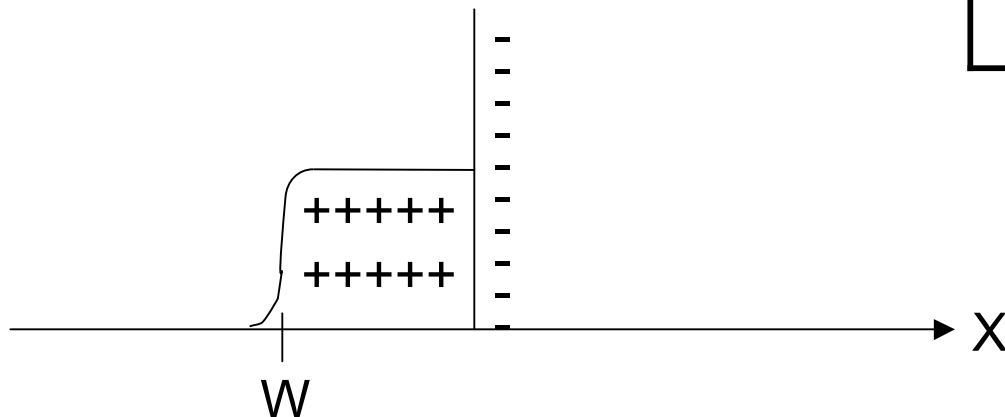
- Charge comes from the easiest thing to ionize, the dopant atoms. This leads to a large region of (+) charges within the semi-conductor.
- In the metal all of the charge goes to the surface. (Gauss's Law)
- The more charge transferred the more band bending.



Depletion Approximation

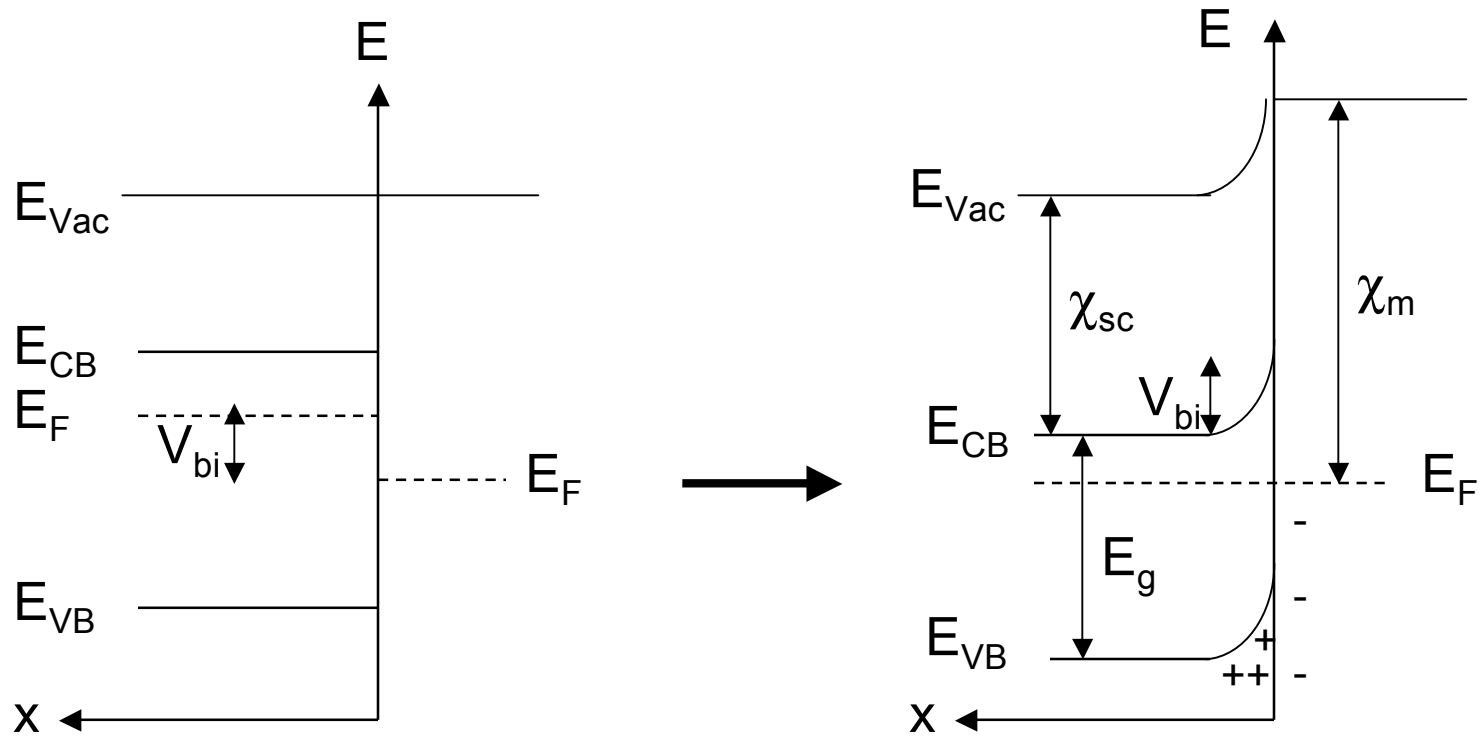
- All donors are fully ionized to a certain distance, W , from the interface.

- $W = W(N_D, V_{bi})$



N_D	↗	W	↘
V_{bi}	↗	W	↗

Final Picture



Useful Equations

$\mathcal{E}(x)$ = Electric Field (V/cm) $\psi(x)$ = Electric Potential (V)

$E(x)$ = Electric Potential Energy (J)

$$\mathcal{E}(x) = -\frac{d\psi(x)}{dx} \qquad E(x) = -q\psi(x)$$

$$\rho(x) = q[p(x) - n(x) - N_A(x) + N_D(x)]$$

Poisson's Eqn:
$$-\frac{d^2\psi(x)}{dx^2} = \frac{\rho(x)}{K\epsilon_0}$$

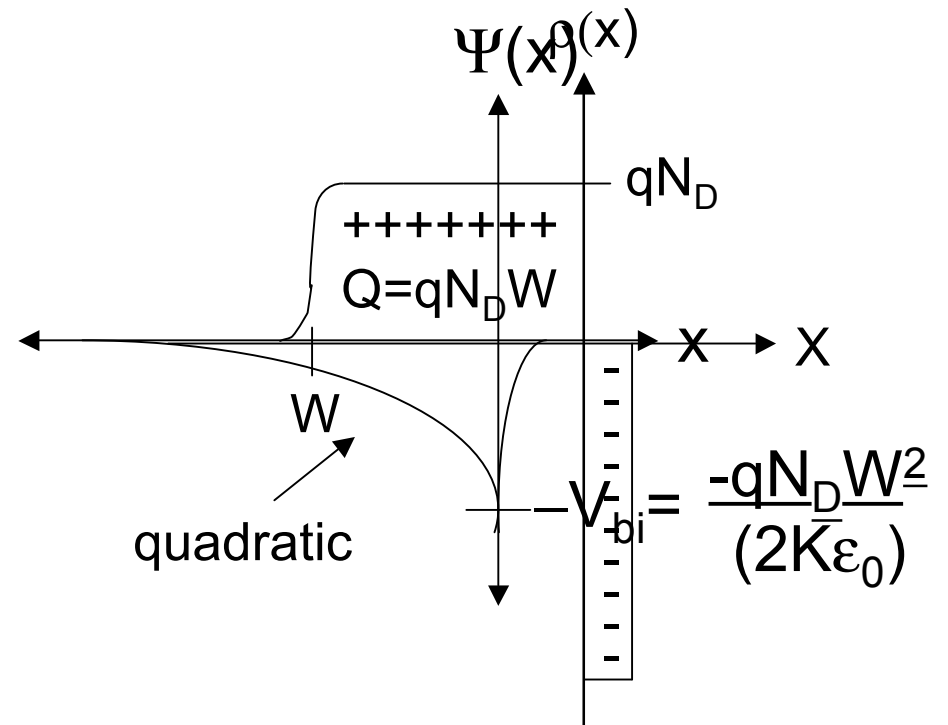
Electric Potential (Ψ)

Integrate Poisson's Eqn.

$$-\frac{d^2\psi(x)}{dx^2} = \frac{\rho(x)}{K\epsilon_0}$$

B.C.'s

$$\begin{aligned} \frac{d\psi(x)}{dx} &= 0 & x &\geq W \\ \psi(x) &= 0 & x &= W \end{aligned}$$



Result:
$$\psi(x) = \frac{-qN_D}{2K\epsilon_0} (x - W)^2$$

Depletion Width

- Rearranging for W:

$$W = \sqrt{\frac{2K\epsilon_0 V_{bi}}{qN_D}}$$

- As expected, W increases w/ V_{bi} and decreases w/ N_D
- If one accounts for the free carrier distribution's tail around $x=W$

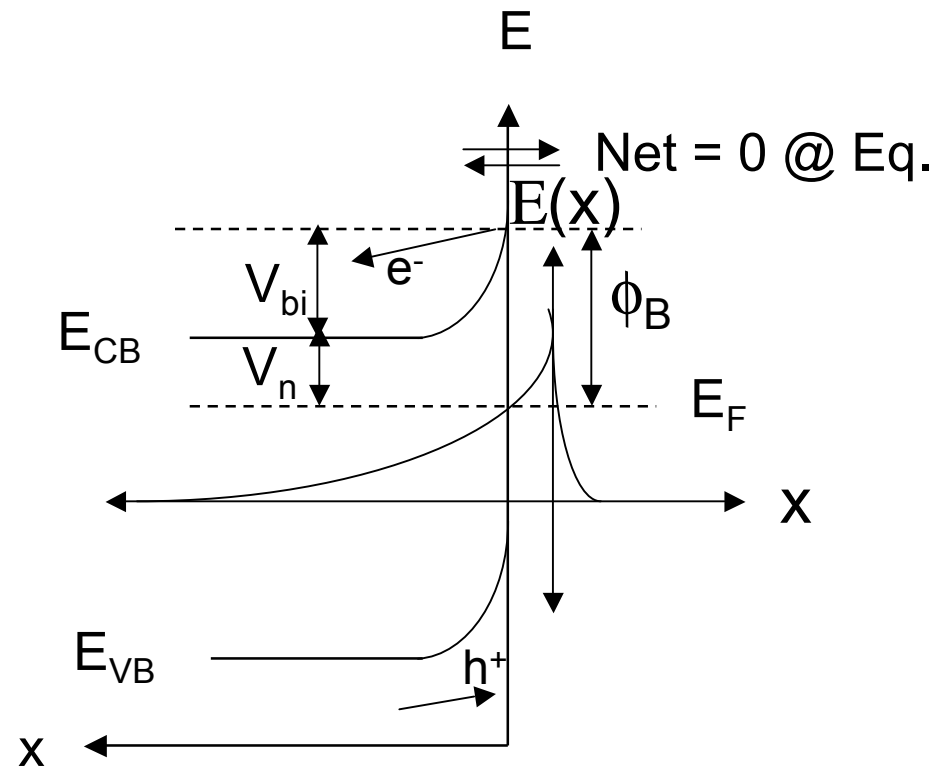
$$W = \sqrt{\frac{2K\epsilon_0 \left(V_{bi} - \frac{kT}{q} \right)}{qN_D}}$$

Typical Values

V_{bi}^{max} (V)	N_D (cm ⁻³)	W (μm)	Q (C/cm ²)
1	10^{13}	11	10^{10}
1	10^{16}	0.36	$3 \cdot 10^{11}$

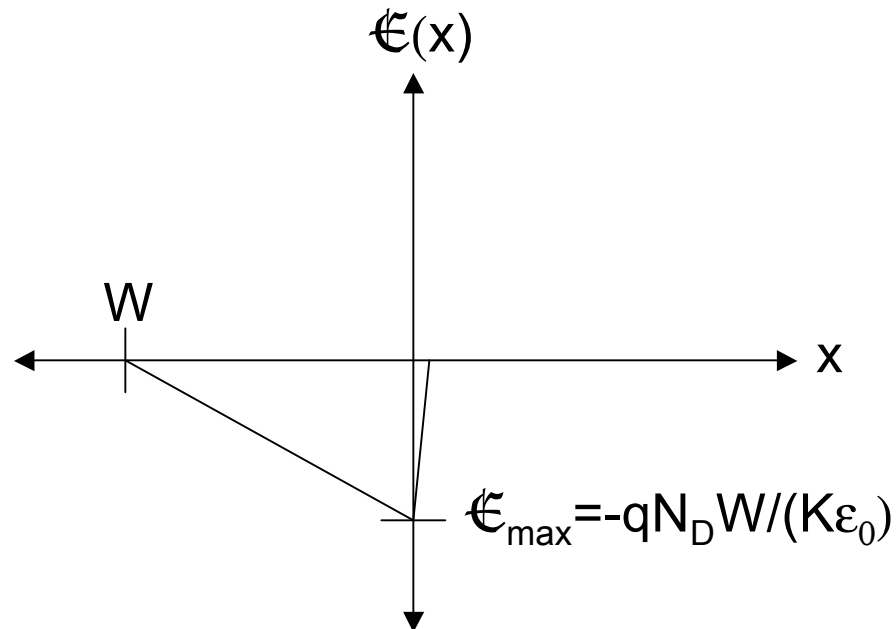
Electric Potential Energy

- $E(x) = -q\Psi(x)$
- $\Psi(0) = -V_{bi}$
- $qV_{bi} = (E_{F,SC} - E_{F,M})$
- $\phi_B = V_{bi} + V_n$
 - Barrier height
 - Independent of doping
 - V_{bi} and V_n are doping dependent

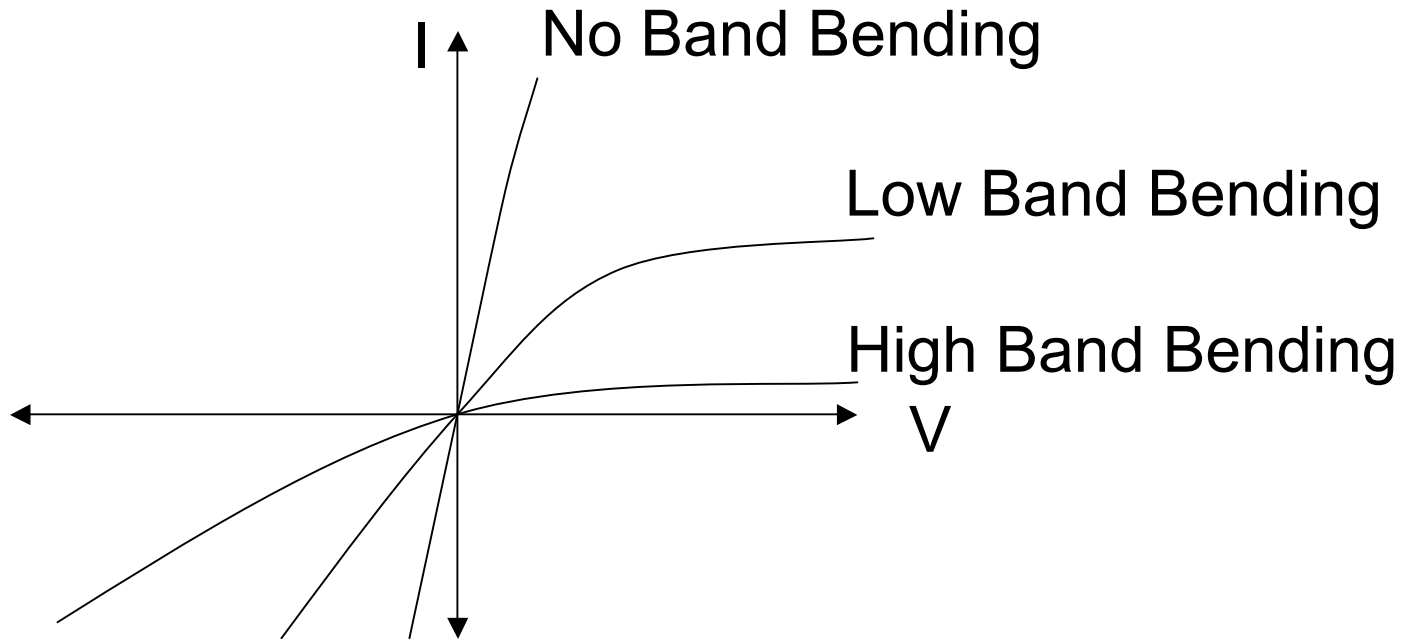


Electric Field (V/cm)

$$\mathcal{E}(x) = -\frac{d\psi(x)}{dx} = \frac{qN_D}{K\epsilon_0}(x - W)$$

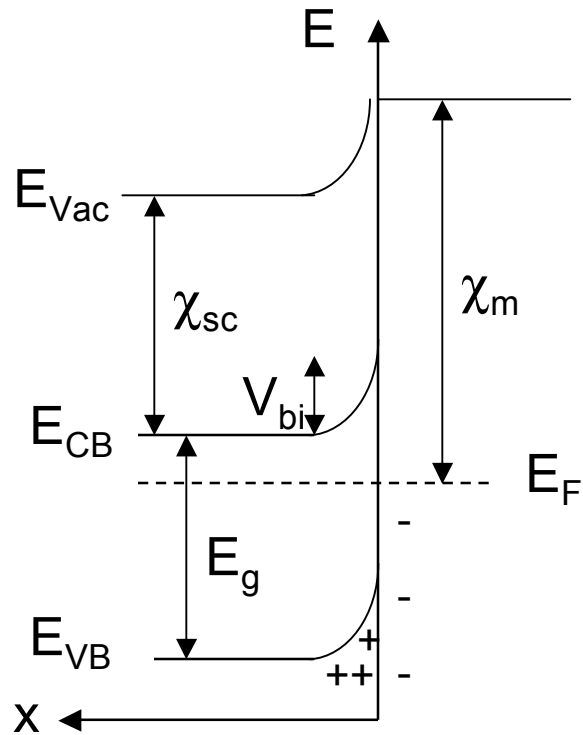


I-V Curve

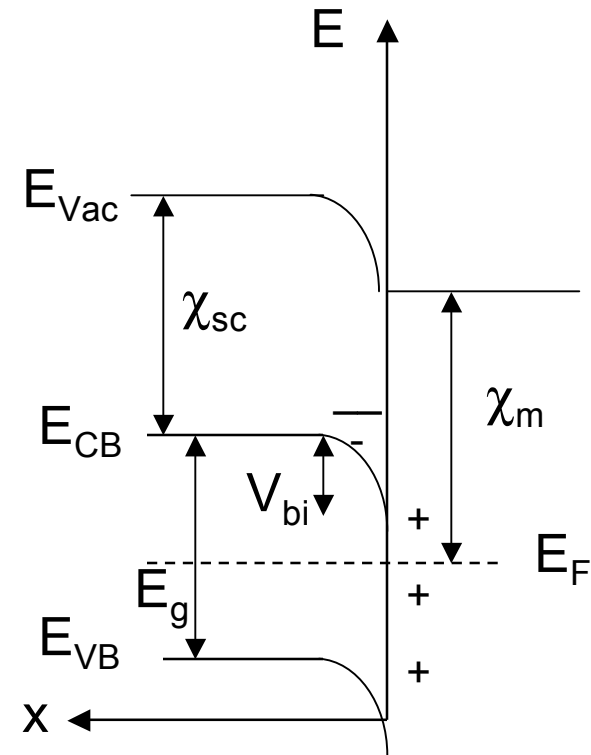


Review

- N-type

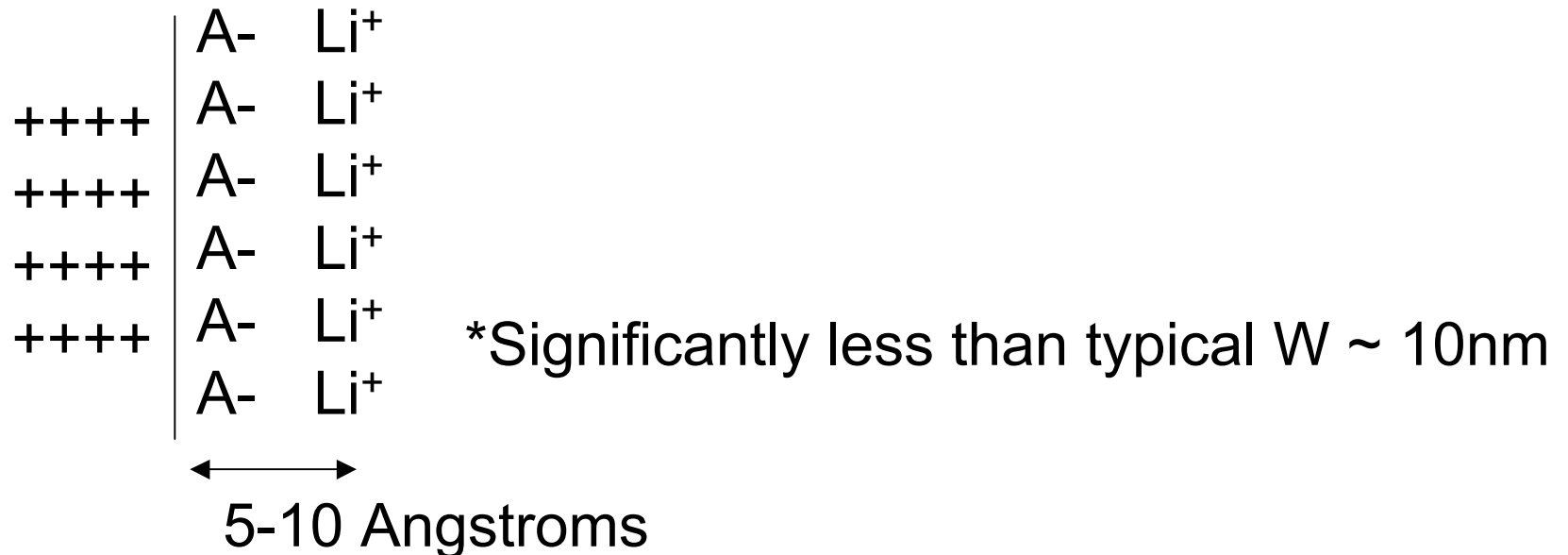


- P-type



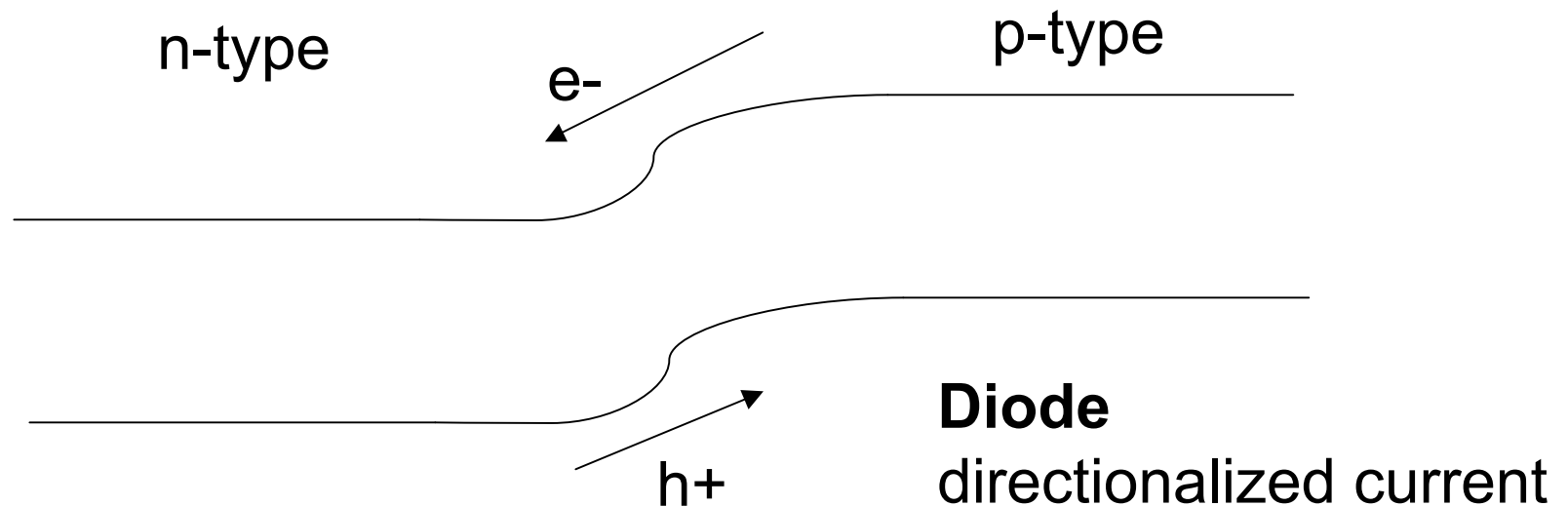
Solution Contact

- 10^{17} atoms in 1mL of 1mM solution
- D.O.S. argument holds
- Difference in exchange current across the interface



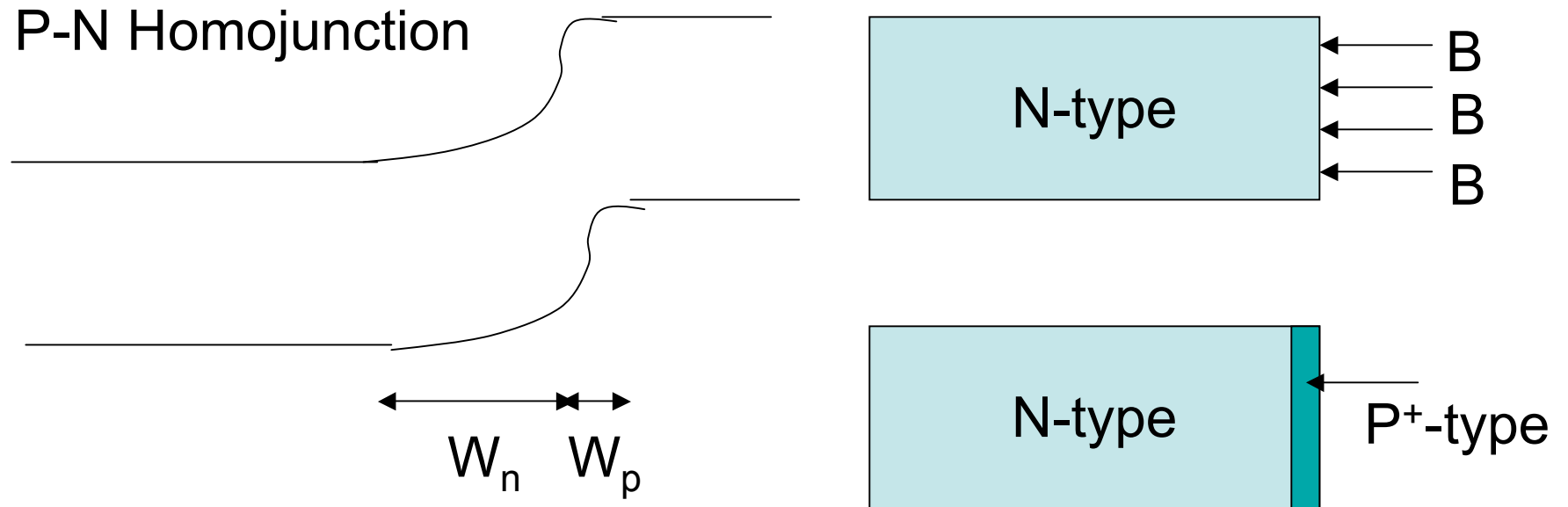
Semiconductor Contacting Phase

- No longer 1-Sided Abrupt Jxn. as the semi-conductor doesn't have infinite capacity to accept charge
- Assume $N_D(\text{n-type})=N_A(\text{p-type})$, then $W_n=W_p$



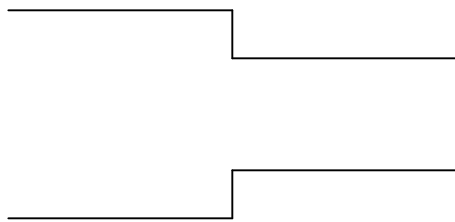
Degenerate Doping

- Dope p-type degenerately
- $N_A \gg N_D \rightarrow$ 1-sided Abrupt Jxn.

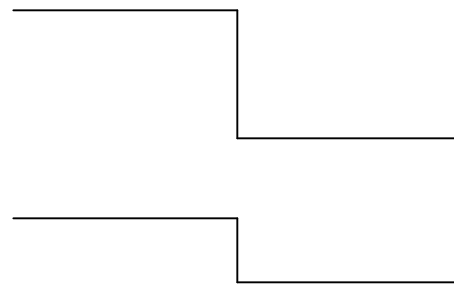


Heterojunctions

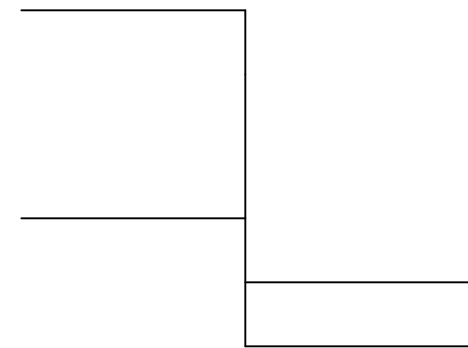
- 2 different semiconductors grown w/ the same crystal structure (difficult)
 - Ge/GaAs $a_0 \sim 5.65$ angstroms



Normal



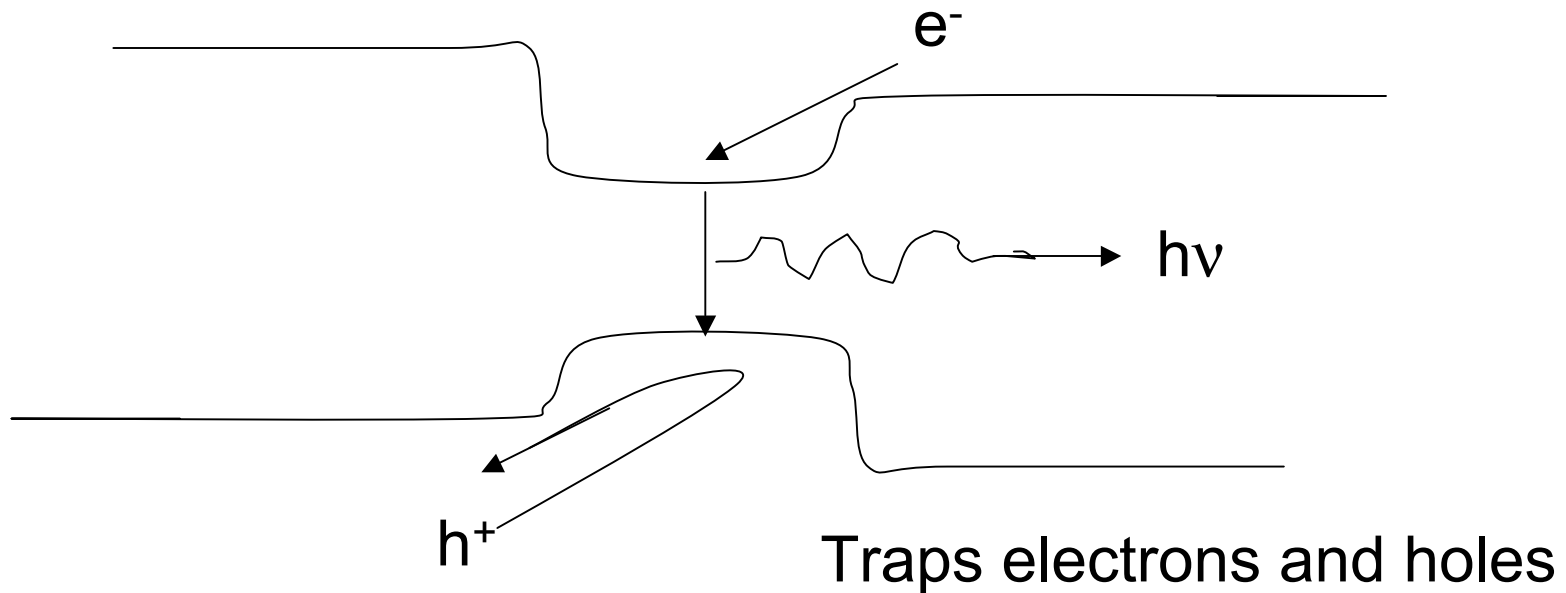
Staggered



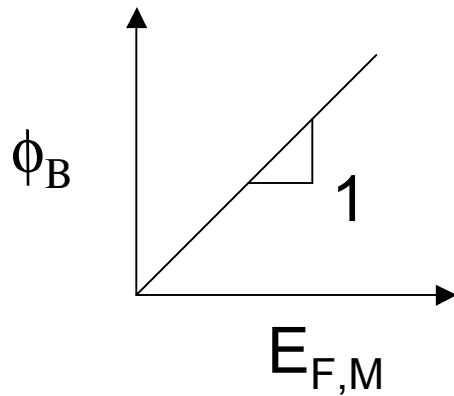
Broken

LASERs

- 3 Pieces --> 2 Heterjunctions
 - p⁻(Al,Ga)As | GaAs | n⁻(Al, Ga) As



Fermi-Level Pinning



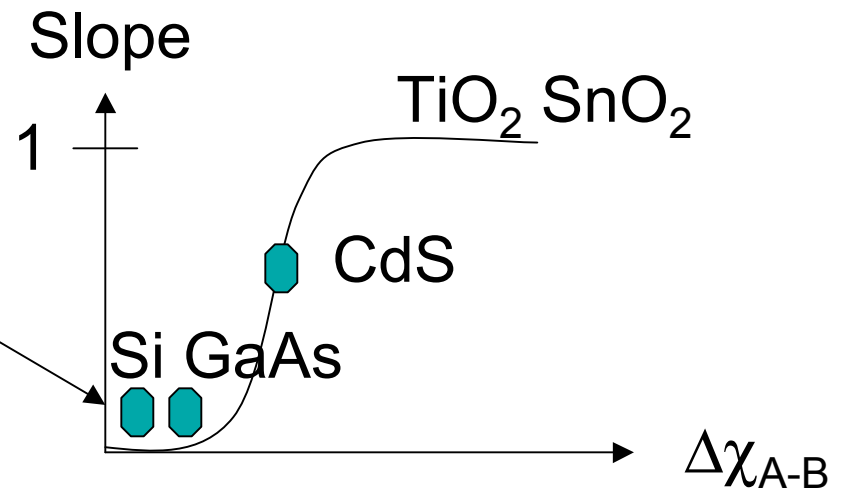
- Ideal Case

(only works for very ionic semiconductors like TiO_2 and SnO_2)

Never works for Si

Fermi-Level Pinning

Sze p. 278

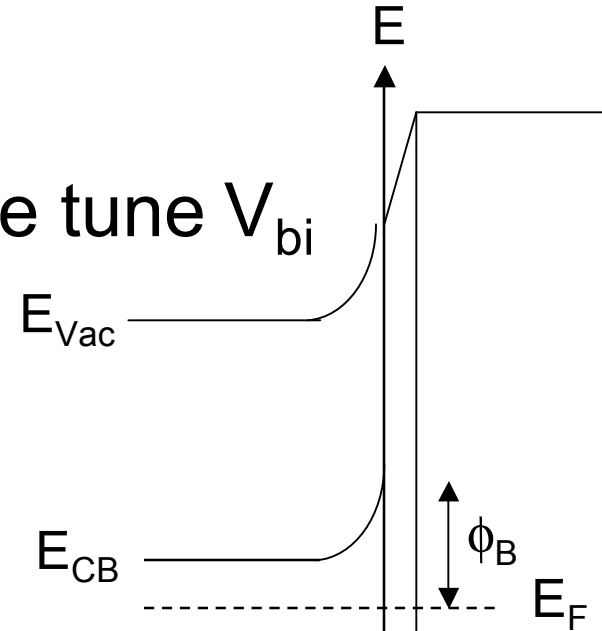
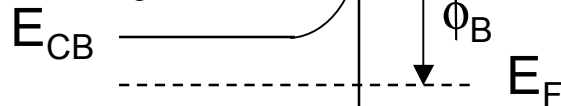


What's Missing?

- Fermi-Level pinning hurts
 - Hinders our ability to fine tune V_{bi}

$$E_{vac} \quad V_{bi/Ni} \sim V_{bi/Pt} \sim V_{bi/Au}$$

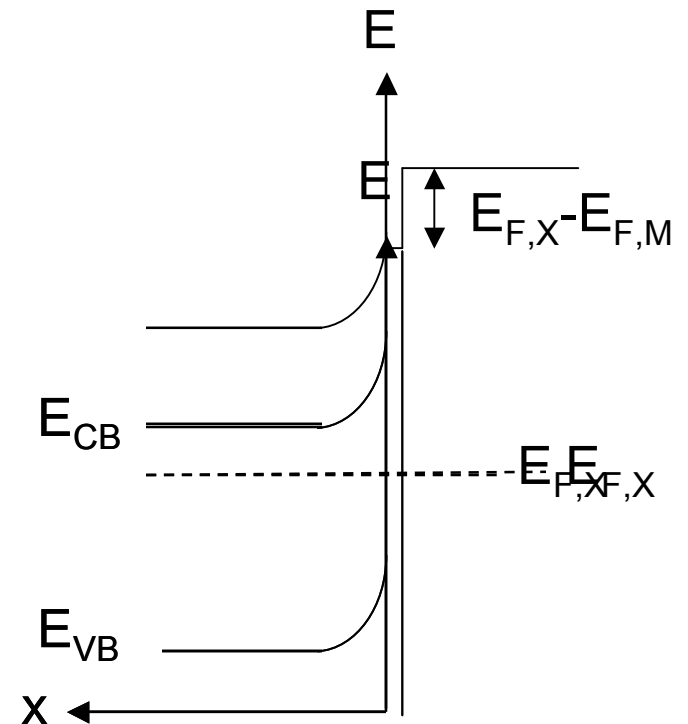
- Why does this happen?



*Solution contact for GaAs sees Fermi-level pinning, while the barrier height correlates well with the electro-chemical potential for solution contact to Si

Devious Experimenter

- Given a Si sample with a magic type of metal on the surface X
- Thus the Fermi-level will always equilibrate to the Fermi-level of X
- Thin interface --> e⁻'s tunnel through it and no additional potential drop is observed



What is X?

- Any source or sink for charge at the interface
 - Dangling bonds
 - Surface states
 - etc.

Questions

- Questions
 - Abrupt 1-sided junction
(What is it?)
 - Sign of Electric P.E. and Electric Potential
(Are they correct? I put them as they were in the notes, but this doesn't seem to agree with the algebra to me)